A COMPARISON OF TWO METHODS OF ADDITION INSTRUCTION, TOUCHPOINTS AND MANIPULATIVES, WITH FIRST GRADE STUDENTS WITH LEARNING DISABILITIES IN A RESOURCE CLASSROOM TO DETERMINE EFFICIENCY AND EFFECTIVENESS

Presented by

LuAnne Littlefield
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ABSTRACT OF THESIS

A COMPARISON OF TWO METHODS OF ADDITION INSTRUCTION, TOUCHPOINTS AND MANIPULATIVES, FOR FIRST GRADE STUDENTS WITH LEARNING DISABILITIES IN A RESOURCE CLASSROOM SETTING

Teachers have increasing responsibilities, which require that skills be taught in the most efficient manner possible. This study compared the effectiveness and efficiency of two methods of teaching simple addition: touchpoints and manipulatives with first grade students with learning disabilities in a resource classroom. Research has demonstrated that both methods are effective. The use of manipulatives was more efficient during the initial stages of instruction but that advantage was lost during the addition of numerals. This study supports the use of touchpoints for greater effectiveness. Also, five of six students preferred the use of touchpoints.

KEYWORDS: Mathematics, Addition, Efficient Instruction, Effective Instruction, Touchpoints, TouchMath, Manipulatives
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By

LuAnne Littlefield

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Director of Graduate Studies

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Date
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THESIS

A thesis submitted in partial fulfillment of the requirements for the degree of Master of Science in the College of Education at the University of Kentucky

By

LuAnne Littlefield

Danville, Kentucky

Director: C. Michael Nelson, Professor of Special Education

Lexington, Kentucky

2003
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ACKNOWLEDGEMENTS

My deepest respect goes to Dr. Mike Nelson for your excellent guidance throughout my graduate program. You required a professionalism I needed, as you demanded data and systematic analysis of behaviors. I still trust my instinct but now back it up with objective supports. I hope to continue learning, growing and reaching for excellence. I’m proud to have had the opportunity to share in your wealth of knowledge.

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My deepest love goes to my family. My husband kept the home fires burning during the many, many hours I attended class and studied at home. You even set a fire under me when I needed a little more motivation. You are the spice I need. My love for my three children overwhelms me. You give me hugs when I need them and even when I don’t. You sympathize when you see the tons of writing revisions I have and no longer complain when I suggest revisions on your papers. This shows you understand the need and the love for learning. I’m thrilled to see you beginning to use the basic concepts of behavior in your day-to-day friendships. I hope you grow to be as wise as your dad.

My deepest thanks goes to my students who participated in this study and others through the years. You have taught me well. Thank you for helping me understand your needs and giving me tons of positive reinforcement. I wake each morning and look forward to seeing you. Thank you for motivating me. When I stop learning and growing, I promise to retire because you deserve the best. You are worth it!
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Chapter One: Introduction

Since the early 1900s, efforts to improve mathematic achievement among students from the United States compared with their peers in other industrialized countries have been part of educational reform movements (Joshi, 1995; Miller & Mercer, 1997a). These efforts include the mathematics standards established by the National Council of Teachers of Mathematics (NCTM) (Flint & Karlsson, 1996). As a result, math standards and corresponding expectations of student performance are increasing.

Students with learning disabilities have more difficulty than peers without disabilities in math computation and problem solving (Miller & Mercer, 1997a). The discrepancies occur among students of all ages. According to Cawley and Miller (1989), the rate of learning for students with disabilities is half that of peers without disabilities.

An extensive body of research addresses strategies for providing instruction in math. The National Center to Improve the Tools of Educators reviewed 956 articles on math research in its report to the California State Board of Education (Dixon, Carnine, Lee, Wallin, & Chard, 1998). Some of the studies reviewed included students with learning disabilities. Although extensive research is available, practitioners must continue to improve and to “fine tune” methods of instruction. As Miller and Mercer (1997a) explain, “Researchers and teachers must continue to work together to determine which curricula and instructional practices will bring about the best results in the shortest amount of time” (p. 54).

With “fine tuning” in mind, the purpose of this study was to address the discrepancy between low mathematics achievement in calculation skills and increasingly
rigorous standards by determining which of two methods of instruction is more effective and efficient for students with a learning disability.

The review of literature includes research articles on math skills of students with learning disabilities of all ages, computation skills of primary students, use of manipulatives, methods of instruction for math computation, and the TouchMath system of computation. The national standards recommended by NTCM briefly are discussed as they affect student expectations. Also reviewed are the positive outcomes of effective instruction for students with behavioral problems. Informational articles also are included that address the issues regarding math standards, critiques of math research, behavior management interventions, and math manipulatives. The literature review was conducted via ERIC On-line, Kentucky Virtual Library, on-line educational journals, and educational web sites. Manual searches were conducted at the university’s educational library. Innovative Research, Inc., the company that produces TouchMath, provided research supporting the use of TouchMath.
Chapter Two: Review of Literature

Math Achievement Among Students with Learning Disabilities

Research suggests that students with mild disabilities lag behind their peers in mathematical calculation and application (Fleischner, Garnett, & Sheppard, 1982; Fleischner, & Manheimer, 1997; Cawley & Miller, 1989; Mercer, 1997; Garnett & Fleischner, 1983). This lag occurs with elementary (Cawley & Miller, 1989; Garnett, & Fleischner, 1983) middle school (Fleischner et al., 1982; McLeod & Armstrong, 1982), and high school students (Warner, Alley, Schumaker, Deshler, & Clark, 1980; Cawley, Baker-Kroczynski, & Urban, 1992; Cawley & Miller, 1989; Greenstein & Strain, 1977). In a survey of middle to high school math teachers by McLeod and Armstrong (1982), teachers reported that students with disabilities lack adequate skills in basic computation and numeration. Middle school students also lack basic addition facts. Fleischner et al. (1982) found that middle school students with learning disabilities have math skills equivalent to those of typical third graders. Garnett and Fleischner (1983) compared the math skills of two hundred forty children, ages 8 to 13, half with learning disabilities and half without disabilities. Their automatization ability and proficiency in basic fact computation were evaluated. The study showed that students with learning disabilities were slower and less proficient than peers without disabilities. Other studies have shown that students with learning disabilities are accurate with regard to basic fact responses but perform more slowly than peers without disabilities. This slower pace may reflect an inefficient use of strategies, such as counting instead of recall (Fleischner, et al. 1982; Erenberg, 1995; Goldman, Pellegrina, & Mertz, 1988). Cawley, Fitzmaurice, Shaw, Kahn and Bates (1979) found that high school students with learning disabilities made
progress, but their progress was slower than that of peers without disabilities. In a later study, Cawley and Miller (1989) found that, typically, these students required 2 years of study to yield a 1-year gain in skill.

National Reform Standards in Mathematic Achievement

According to the U.S. Department of Education’s Office of Educational Research and Improvement (Campbell, 2000), math scores declined among students nationwide from 1973 to 1982. This decline was supported in a report, *A Nation At Risk*, in April 1983 by The National Commission on Excellence in Education. Although studies completed by the U.S. Department of Education (Campbell, 2000) show an increase in student scores since 1982, concerns of student progress nationwide compared with students in other nations, continue to exist (Gonzales, 2000). Among the many efforts to reform math instruction, national standards have been one reaction to poor student performance nationwide. The NCTM standards stress instruction based on problem solving strategies used in students’ daily lives rather than abstract operations, rote memorization, drill and practice (Mercer, 1997; Flint & Karlsson, 1996). The NCTM developed the following goals:

- Students learn to value mathematics
- Students become confident in their abilities to do mathematics
- Students become mathematical problem solvers
- Students learn to communicate mathematically
- Students learn to reason mathematically (Flint & Karlsson, 1996, p. 4)
Flint and Karlsson (1996) support the standards and explain, “Manipulatives, calculators and computers are tools that enable students to explore concepts and number patterns, analyze data rather than memorize a series of steps and perform drills on paper” (p. 5). Other researchers disagree with the standards and suggest best practice as defined by other research is being ignored (Mercer, 1997). Dixon and Carnine (1990) argue the NCTM standards fail to emphasize pedagogy, the instructional delivery system, and implementation. Miller and Mercer (1997a) suggest “enough knowledge has been gathered to move math educators into a ‘refining’ rather than a ‘reforming’ mode” (p. 33). It is not the purpose of this review to debate this issue, but to point out the differences in the views of researchers.

*Rationale for Learning Facts*

*Basic facts.* Although the NCTM standards do not specifically list mastery of basic math facts, there is support for teaching these skills. Mercer (1997) explains the logical structure of math as it builds from simple relationships to more complex tasks. In a study of multiplication and division, Miller and Milam (1987) discovered that errors in multiplication primarily were due to a lack of basic addition skills and memorization of multiplication facts. Miller and Mercer (1997b) explain that students who lack mastery of basic facts will experience failure at higher-level thinking skills. Dixon (1994) stresses that teaching the four basic operations (addition, subtraction, multiplication, and division) is essential to any math curriculum. Basic addition skills are essential to the foundation of all math skills.

*Levels of instruction.* Mercer (1997) discusses the basic levels of teaching math according to Underhill: concrete, semi-concrete, and abstract. Manipulatives are used at
the concrete level to improve the student’s understanding of the mathematical process. Manipulatives are defined as “objects or things that appeal to several of the senses” (Yeats, 1991, p.7) and have been used in math instruction since the 1930s (Sowell, 1989). Manipulatives have been used effectively for third grade students with learning disabilities (Marsh & Cook, 1996), fourth graders with learning disabilities (Jones, Thornton, & Toohey, 1985), at-risk students in grades four through six (Bryet, 1992), junior high students (Threadgill-Sowder & Julifs, 1980), and students in kindergarten through grade eight (Suydam & Higgins, 1977). Some research has indicated possibly inappropriate uses of manipulatives as some students use the manipulatives mechanically instead of meaningfully (Baroody, 1989, p.4). Mercer (1997) defines the semi-concrete level as the use of materials that include dots, lines, tallies, pictures or any visual model. According to Mercer (1997), the abstract level involves use of numerals in computation.

Instructional Strategies for Teaching Math

Mercer, Jordan, and Miller (1994) emphasize that teachers must be aware of individual student needs and design instructional strategies that address those needs. Research supporting this statement includes that of Threadgill-Sowder and Julifs (1980), who found that manipulatives helped low achieving junior high school students but slowed the progress of “more able” students (p. 363). Baroody (1989) was critical of manipulatives because pupils can learn to use manipulatives mechanically to obtain answers, just as with symbols. He observed that the particular medium used (objects, pictures of objects, or video displays of pictured objects) may be less important than that the experience is meaningful to pupils and they are actively engaged in thinking about it. Evans and Carnine (1990) also suggest that instruction is necessary to ensure that both
procedural and conceptual knowledge are developed. Evans and Carnine as well as Scott (1993) suggest bypassing the concrete stage and teaching math computation using a semi-abstract method of instruction.

Scott (1993) used TouchMath, a multi-sensory program from Innovative Learning Concepts, Inc., with three elementary students: one with learning disabilities, one identified with mild mental disability, and one with moderate mental disabilities as outlined by Georgia’s criteria for identifying students with special needs. In TouchMath, the student uses dots on each number for counting forward or backward. Appendix A shows all numerals with touchpoints. The skill areas include column addition, two-digit addition with regrouping, single-digit subtraction, two-digit subtraction, and two-digit subtraction with regrouping. A multiple-probe design across math skills was used. The phases were initial screening, probe conditions, touchpoint training, and intervention. These phases were implemented with each subject individually for 15 to 30 minutes. After baseline was complete, the trainer taught the students the touchpoints on the numerals until they reached 100% mastery. Then math computation with the use of touchpoints began. The trainer modeled calculation steps with touchpoints and supervised guided practice. The probes consisted of 20 math problems used in the training phase but the problems did not have touchpoints. All students made progress when using touchpoints and met criterion. One student maintained 100% accuracy on 3- and 6-week maintenance probes and generalization. The last data on the other two subjects were four probe sessions immediately following a training phase. One student was 100% accurate on column addition and three-digit subtraction, while demonstrating an accuracy of 89% on double-digit subtraction. This was an improvement from 0% accuracy in baseline. The
last student, whose baseline data ranged from 0% to less than 40% accuracy, demonstrated 100% accuracy on all three skill areas.

Kokaska (1975) used a manual notation system to teach addition and subtraction to four primary students with mild mental disabilities. This system used dot notation for counting in addition and subtraction. These female students (ages 9, 12, 12, 13) previously had demonstrated their inability to learn the math skills from the regular curriculum materials and being taught individually. Three students continued to draw the dots on the numerals in order to solve the equation. The students increased their accuracy in addition even though the difficulty of computation increased from single digit addition to double digit and column addition. One student progressed farther by only visualizing the dots to compute addition, subtraction, and beginning multiplication problems.

Kramer and Krug implemented a system like TouchMath, which uses a dots-on-numerals system to teach basic math concepts to students with various disabilities (learning disability, educable mentally retarded, language disability, trainable mentally retarded, educationally handicapped) from kindergarten to second grade. The students progressed through four different stages: counting each bold dot on the numerals; counting each faded dot on the numerals; starting with the top numeral and adding by counting the faded dots of the bottom numeral; and converting to rote facts. Each student progressed through these phases at his/her own rate. Kramer and Krug (1973) found this system benefited students who were beginning to learn math concepts, students having difficulty, or students who would rely on a manipulative system throughout their lives.

Evans and Carnine (1990) compared two types of instruction—concrete and semi-concrete—to determine which was more effective and efficient. They compared two
commercial texts: *Explorations* by Addison-Wesley, which uses manipulatives, and *Connecting Mathematics Concepts*, which use an algorithm strategy. The results were similar throughout posttest and maintenance conditions. Each strategy was comparable to the other in terms of accuracy. Evans and Carnine were surprised that the scores were so low (68% and 60% accuracy respectively), considering the amount of time spent in instruction. A significant difference was established in efficiency. Instruction with concrete manipulatives took longer than the algorithm strategy.

**Implications for Instruction with Students with Behavioral Problems**

“Low achievement and behavior problems go hand in hand; they are highly related risk factors” (Kauffman, 1997, p. 247). Kauffman describes a study by Kupersmidt and Patterson that reported a direct correlation between students with three or more social problems and low achievement. Other researchers stress the importance of increasing the academic skills of students with behavior problems as a strategy for decreasing discipline concerns (Ayllon & Roberts, 1974; Kerr & Nelson, 2002).

Good instruction is now known by researchers to be the first line of defense in behavior management. That is, a good instructional program prevents many behavior problems from arising, and an emphasis on instruction is compatible with the clearest mission of public schools (Kauffman, 1997, p. 91).

When teachers have access to two instructional procedures that use strategies with proven effectiveness, it seems desirable to determine which procedure is more efficient. Neither the student nor the teacher has time to waste in school. Mercer et al. (1994) warn that the poor math progress of students with learning problems and the likelihood of
higher standards establishes a clear need to improve math instruction. Without better math instruction, these students will continue to face debilitating frustration and failure.

*Purpose of the Research*

Teachers of students with disabilities constantly must strive for effective and efficient instructional methods. The purpose of this study was to determine which method of instruction—semi-concrete using TouchMath, or concrete using manipulatives as outlined in *The Path to Math Success*—is more efficient when teaching addition to primary students with learning disabilities. The district-adopted math program is Silver Burdette Ginn’s *The Path to Math Success* (Fennell et al., 1998). This study attempted to answer the following questions:

1. Which is more effective, TouchMath or manipulatives, in teaching basic addition facts to students with learning disabilities?
2. Which is more time efficient, TouchMath or manipulatives, in teaching basic addition facts to students with learning disabilities?
3. What are students’ opinions of TouchMath and manipulatives?

Effective and efficient instruction is needed to assist students with learning disabilities acquire academic skills in a timely manner. The answers to these questions are one step towards improving instruction for students with learning disabilities.
Chapter Three: Methods

An adaptive alternating treatment design was used to compare two methods of instruction. Three sets of addition problems were developed with different numerals in each set. Two of the sets represented the methods of instruction for comparison, while the third was a control set. Daily probe data was gathered on students’ rate of correct digits per minute. Following initial baseline probes across all three sets, the design was implemented across three conditions. In the first condition (Strategy 1), each method of instruction was taught using the longer method. The student was required to count (via touchpoints or manipulatives) both numerals in the addition problem. The second condition (Strategy 2), involved teaching a quicker method of adding, in which the student said one numeral aloud and added (via touchpoints or manipulatives) the next numeral.

When using the touchpoint method for Strategy 1, students had to touch the touchpoints on both numerals and count. One set of addition problems were used with touchpoints while a different set of addition problems was used with manipulatives. When using manipulatives for Strategy 1, students put round colored counters beside both numerals and counted them together.

With Strategy 2 touchpoints, the student had to say the large numeral, and then touch the touchpoints of the smaller numeral to count. Similarly, when using manipulatives in Strategy 2, the student placed the colored counters next to the smallest numeral, said the large number, and added by counting the counters.

While students were applying the methods to respective sets of problems, daily probe data was gathered on each set, as well as on the control set. In the third condition,
the most effective method of instruction, as documented by comparing data between touchpoint method and manipulative method, was applied to this control set.

Participants

Six primary students, identified by the school district as having disabilities under the Individuals with Disabilities Education Act, participated. All students and were receiving resource assistance in math, After parents were notified and permission was granted, they were asked to resist from tutoring their children in math. Student prerequisite skills included rote counting to 18, one-to-one correspondence to 18, fine motor skills to touch each point, write numerals to 18, and stable school attendance.

Several students received free or reduced school lunch, which is one measure of socioeconomic status. With the exception of one student, intelligence was defined as the full-scale intelligence quotient determined by the Wechsler Intelligence Scale for Children, third edition (WISC-III). The sixth student (Michael) had been assessed at age 4 on the Battelle Developmental Inventory, and was diagnosed a having a developmental delay disability. Five of the students had behavior goals written in the Individualized Education Plan (IEP). Following directions, stay in assigned area, and stay on task were some of the objectives.

Special education diagnostic label (SE Label) and specific academic achievement were determined by results of an evaluation completed by the school psychologist for each student’s initial placement or re-evaluation by his IEP team. Each student also had academic delays in other areas. Placement level and hours of special education services were determined by committee, which developed individual education plans. Each student participated in the regular classroom except for the resource time listed. Table 1
summarizes the students’ characteristics.
<table>
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<tr>
<th>Name</th>
<th>Gender</th>
<th>Age</th>
<th>Ethnicity</th>
<th>Eligible for free or reduced lunch</th>
<th>IQ</th>
<th>SE Label</th>
<th>Specific Academic Achievement in Math</th>
<th>Grade Level</th>
<th>Level of Special Education Placement</th>
<th>Daily Time in Special Education Placement</th>
<th>Behavior Goals on IEP</th>
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<td>Keith</td>
<td>M</td>
<td>6</td>
<td>Anglo</td>
<td>no</td>
<td>61</td>
<td>mild mental disability</td>
<td>mild delay</td>
<td>1</td>
<td>Resource</td>
<td>2.5 hrs</td>
<td>no</td>
</tr>
<tr>
<td>Doug</td>
<td>M</td>
<td>6</td>
<td>Anglo</td>
<td>yes</td>
<td>83</td>
<td>learning disability</td>
<td>mild delay</td>
<td>1</td>
<td>Resource</td>
<td>1.5 hrs</td>
<td>yes</td>
</tr>
<tr>
<td>Rye</td>
<td>M</td>
<td>6</td>
<td>Anglo</td>
<td>no</td>
<td>81</td>
<td>other health impaired</td>
<td>mild delay</td>
<td>1</td>
<td>Resource</td>
<td>2 hrs</td>
<td>yes</td>
</tr>
<tr>
<td>Richard</td>
<td>M</td>
<td>6</td>
<td>Anglo</td>
<td>yes</td>
<td>98</td>
<td>learning disability</td>
<td>mild delay</td>
<td>1</td>
<td>Resource</td>
<td>1 hr</td>
<td>yes</td>
</tr>
<tr>
<td>Michael</td>
<td>M</td>
<td>6</td>
<td>Bi-racial</td>
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<td>n/a</td>
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<td>Resource</td>
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<td>Tim</td>
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<td>yes</td>
<td>69</td>
<td>mild mental disability</td>
<td>mild/ moderate delay</td>
<td>1</td>
<td>Resource</td>
<td>2 hrs</td>
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</table>
The researcher was an elementary special education teacher with thirteen years experience teaching children with disabilities. She also had many years of experience teaching addition using Touch Math procedures and manipulatives. The researcher was completing the final requirements for a Master’s degree in Emotional and Behavioral Disabilities. The researcher implemented daily lessons, collected student data, and summarized the information outlined in this study.

Two staff members participated as data collectors. One was a certified special education teacher with 9 years experience working with students with disabilities. The second person assisting was the instructional assistant for special education. She was completing the final requirements for an undergraduate degree in special education. These staff members documented the reliability of instruction and student responses.

Setting

All students attended public elementary school in a small county the Southeast with a population of 27,612. The school had a population of 620 students preschool through fifth grade.

Instruction occurred in a small group setting in the resource room. Students sat around the semi-circle of a kidney-shaped table as the instructor sat in the cutout section. Instruction and probe sessions were implemented in a group setting with the six participants.

Materials

Instruction via one set of addition problems dedicated to one of 3 procedures, was implemented daily at the same time of day. The set to be implemented each day was determined by random drawing. A piece of paper with one set of problems was placed in
a container. A paper was drawn out and that set was written on the calendar. When all three pieces of paper were drawn, all went back into the container to be drawn again. This continued until three months of implementation was scheduled.

There were three different probe worksheets for each set. These were used consecutively. Each session lasted 15-20 minutes. During daily probe sessions, students were seated separately throughout the room to complete the worksheet independently.

Appendix B lists the addition problems in each set. No numeral appeared in more than one set. Appendixes C, D, and E present one sample worksheet for each set. These were used for probe assessments, which included the control set. The math problems for each probe assessment were randomized to attempt to reduce the threat to internal validity of a child memorizing the test. For baseline conditions, the probe worksheets were used.

Individual addition problems for student use during the instructional sessions were written on 2 in. by 11 in. strips of paper with six replications of one addition problem. Each addition problem was on a separate strip of paper. The font style was Primary One with a point size of 36. During the TouchMath phase, two strips of problems were available—one with touchpoints and one without. Manipulatives (one inch round colored counters) were used for the problems in Set B.

A stopwatch/timer was used to document all conditions: instructional, probe, maintenance, and generalization. Established classroom reinforcers were planned for use during this study and were readily available. These reinforcers included using the “magic wand” to recognize students on task, granting free play time when academic tasks were completed early, and competing in the “Good Behavior Game” (Kerr & Nelson, 2002).
The students responded positively to the structure and methods introduced. Only Doug needed to follow the rule for completing the probes, which was that neither touchpoints nor manipulatives could be used in solving the problems. During two probe sessions for the control set, Doug was observed using touchpoints when he was not allowed. He created his own touchpoints for numerals one and four. When reminded not to use touchpoints, he stopped. No other behavior intervention was needed for any child. Positive reinforcement was effective.

Data Collection

Three probe worksheets were developed for each method of instruction so students would not memorize the answers. Each worksheet was labeled A, B, and C. The use of worksheet A would be repeated only after B and C worksheets and probe worksheets from the other methods of instruction were used, which occurred approximately every 9 days. Twenty problems were presented on each side of the worksheet for a total of 40 problems. The back was a duplicate of the front. The students gave no indication they recognized this duplication as no student turned the probe worksheet over for an answer.

Each worksheet had addition problems placed in random order. Of the nine problems, three were repeated six times, five were repeated four times, and one was repeated twice. This unequal representation of addition problems is a limitation of this study.

Nine numerals were sorted into three sets. Each set was paired with a method of instruction. Numerals nine and one were grouped into Set C. Having the easiest numeral (one) and the hardest numeral (nine) in the same set potentially interfered with the equivalency of the three sets. The other two sets are as equivalent as possible using
numerals two through eight.

Each of the three sets had nine different addition problems with 20 on each side. Another way in which the facts were controlled was two sets had nine single digit answers and one set had 10 single digit answers. The sums were counterbalanced as two sets had two addends five or above and two sums below five. Set C had one sum above five while three were below five. These three sets were functionally independent of one another, as there was no repetitive use of an addend.

Probe sessions were conducted daily at the beginning of the class prior to instruction. When signaled to begin, the group of students had one minute to answer as many problems as possible. The number of digits correct in this one-minute timing determined the rate correct. The number of correct digits written per minute was recorded for comparison (Mercer, 1997). Data also were collected on students’ correct use of touchpoints. The only responses possible were correct, incorrect or no response. The social validity of each method was assessed via student interviews.

Procedures

General procedures

The researcher implemented both methods of instruction, control set, and all probe sessions to reduce threats to internal validity due to instrumentation. Simple addition was taught using two methods: TouchMath and manipulatives.

Baseline. Baseline data consisted of one 1-minute probes for each instructional method and the control set. Worksheets for daily probes were used to collect baseline data. Students were reminded to not use tally marks or their fingers. Prior to baseline, each student’s fine motor skills were assessed to determine the rate of numerals per
minute a student could write. Students wrote numerals zero to nine as many times as possible in one minute. Their rates ranged from 44 to 64 numerals per minute.

Intervention. During instruction, one method of instruction was implemented daily. The instructional methods and the control set were rotated through sessions in random order to reduce possible multiple treatment interference. When the probe was addition with touchpoints, the day’s instruction was on addition with touchpoints. When the probe was addition with manipulatives, the instruction was addition with manipulatives. When the probe was the control set, the day’s lesson was a review of math skills not related to this study. This review included creating patterns, counting money, identifying fractions, skip counting, and orally solving story problems. The time allowed for his review day was equivalent to that for each other method.

Each session began with a timed probe session. When needed, the instructional sessions began with a simple finger play used to quiet the group. This finger play was adapted from one recommended by Jean Feldman (1995). If a student failed to participate in any activity, the regular classroom discipline procedure was implemented (see Appendix F for classroom discipline procedure). The discipline procedures were based upon methods from Harry Wong’s (Wong & Wong, 1998) First Days of School and Tim Phelan’s (1995) 1-2-3 Magic: Effective Discipline for Children 2-12. No discipline intervention was needed. All students participated willingly and responded positively to the structure and methods introduced. Other than reminding Doug to not use his inventive touchpoints for the control set, no behavior problems occurred.

Probe sessions. Probe sessions for addition with touchpoints (Set A) and addition with manipulatives (Set B) occurred prior to instruction (see Appendix G for the
reliability of student response data collection form used for baseline and probe sessions). Probe sessions occurred daily after the first instructional session. The probe worksheets consisted of addition problems in the individual sets. The problems on the worksheet were randomized. In order to document the correct number of digits per minute, each probe session was one minute in duration.

**General Procedures for Touchpoints**

*Touchpoint acquisition.* The researcher guided the students using an antecedent/prompt/test method (Wolery et al., 1992) to teach the position of the touchpoints. Instruction for teaching touchpoints was described in Bullock’s (1998) *TouchMath First Grade Counting Kit Guide*. This instruction time was documented. The numerals, which were introduced with touchpoints, were two, five, and eight (see Appendix A for a description of the touchpoints for all numerals).

The researcher displayed the numeral two with touchpoints and modeled the proper method for touching and counting the touchpoints. The students then imitated the correct method using number two with touchpoints. Next the researcher demonstrated the same method but the numeral did not have the touchpoints printed on it. Criterion for mastery was for the student to use the correct method of counting with touchpoints even though the numeral did not have printed touchpoints. Each numeral was taught to a mastery criterion of 100% accuracy on 5 consecutive trials prior to the introduction of the next numeral. Also, all students were required to meet criterion for mastery before a new numeral was introduced to the group. Students continued to practice touching the correct pattern until all had met criterion. A maximum of two numerals were taught in each session. Any student who did not reach criterion received tutoring at a time other than
during established sessions. Keith was the only student needing extra time. He required 1 additional minute to master touchpoints for numeral five. When touchpoints were used with the control set, he needed 1 additional minute to master numeral nine. When the students met criterion for the three numerals, instruction on addition with touchpoints began (see Appendix H for data sheet).

*Intervention: TouchMath strategy 1.* Bullock (1998) encouraged teaching students TouchMath addition in a progressive sequence. Therefore, addition began with numerals two and five and followed the sequence outlined in each set. The method for teaching TouchMath addition followed the guidelines in the kit (Bullock, 1998) and used an antecedent, prompt, and test model (see Appendix I for a sample lesson plan.) Instruction with touchpoints on the numerals continued until all students demonstrated 100% accuracy (counting the touchpoints correctly for 3 consecutive trials). Then the students practiced adding the same problems, touching their fingers on the appropriate points even though the touchpoints were not marked on the numerals. Mastery was defined as adding the problem correctly for three consecutive trials. After all students mastered one problem, the next problem was introduced. A maximum of two addition problems could be introduced in one session. If any student performed below 60% accuracy on the probe session, touchpoint addition for those problems was retaught. Instructional time was documented. Keith required 4 additional minutes learning the fact 2+5, 4 additional minutes to master 5+2, and 2 additional minutes learning 2+8 for a total of 10 minutes. He did not need extra time for the other six addition problems. Keith’s additional tutoring sessions occurred when other students had a few minutes free time (which they spent quietly reading a book or practicing math problems) during math class or after they had
left the resource room. This tutoring was accomplished in two sessions. After all students mastered all addition problems, the second strategy was implemented.

**Strategy 2.** The second strategy was a faster method of adding in TouchMath. This step taught the students to use touchpoints in a more efficient manner. Students were taught to say the largest number and add on using touchpoints. For example, if the addition problem was 8+5, students were taught to start with eight and count up while using touchpoints on numeral five: Say 8, and count on 9, 10, 11, 12, 13.

**General Procedures for Manipulatives**

*Intervention: manipulatives strategy 1.* An antecedent, prompt, and test strategy was used to teach students how to use three-dimensional manipulatives in solving addition problems. The students already had the prerequisite skill of one-to-one correspondence. Students gathered the appropriate number of single colored counters to match one number, gathered another colored counter for the second number, combined (added) the manipulatives, and determined the answer. For example, if the problem was 3+6, the student counted three red counters, six blue counters and combined them for the answer (Fennell, Ferrini-Mundy, Ginsburg, Greenes, Murphy, & Tate, 1998). A sample lesson plan is provided in Appendix J. Mastery was defined as adding the problem correctly for three consecutive trials. After all students mastered one problem, the next problem was introduced. A maximum of two addition problems could be introduced in one session. When all students met criterion, the manipulatives were removed and the students practiced the same problems. Following directions from the teacher’s manual *The Path to Math Success*, the researcher encouraged them to draw a picture (circles) to represent the numeral (Fennell et al., 1998). They were not allowed to count on their
fingers, make tally marks, or use any other technique. Although tally marks are a semi-concrete level of math similar to drawing circles, this study only encouraged drawing circles as recommended by the teacher’s manual. When all students completed the problem correctly on three consecutive trials, another addition problem was taught. Keith required 4 addition minutes to master 3+6, and 3 more minutes to learn 6+3 for 7 extra minutes. Tutoring occurred during math class when the other students had a few minutes of free time or after they left the resource classroom. Keith did not need any extra time for the other seven addition problems. After all students mastered all addition problems, the second strategy was implemented.

**Strategy 2.** The second strategy is a faster method of adding with manipulatives. The students were taught to add using manipulatives using a shortcut as outlined in the teacher’s manual *The Path to Math Success*. For example, if the problem was 6+3, the student put three manipulatives beside the numeral three. The students said the numeral six and counted up as they used the manipulatives. The researcher modeled the correct method by placing manipulatives by the smaller number, saying the largest numeral and counting the manipulatives of the smaller numeral. Students then demonstrated understanding by performing the procedure. Any errors were immediately corrected and students practiced the correct procedure.

As described earlier, probe sessions occurred prior to instruction and consisted of addition problems limited to Set B. The problems on the worksheets were randomized. Although no manipulatives, tally marks, or touchpoints were used during one-minute probe sessions, students could draw circles to help add. No student was observed using touchpoints or tally marks.
**General Procedures for Control Set**

*Daily probes.* Probes for the control set consisted of one-minute sessions. The students were reminded to not use fingers, tally marks, or touchpoints. No instruction on addition occurred. The students received instruction on math concepts unrelated to this study. One student, Doug, attempted using touchpoints on two occasions—probe 31 and 33. He stopped when directed; however, this may have increased his number of digits correct for those sessions.

*Touchpoints and Set C.* Data collected during probes for Set A and Set B demonstrated that a higher rate of correct numerals per minute occurred when one method of teaching addition was used. That method was implemented with Control Set C addition problems.

The plans for maintenance and generalization are noted but were not implemented because the school year ended. The intervention strategies continued to the last week of school.

**Experimental Design**

An adapted alternating treatment design (Sindelar, Rosenberg, & Wilson, 1985) was used to assess the efficiency of the two instructional procedures. Comparisons were made across strategies (touchpoints and manipulatives) and participants. A control set was added to the procedures to strengthen experimental control. Similarities across instructional procedures, sets of addition problems, reinforcement and discipline procedures, as well as randomized worksheets and counterbalanced times for instructional sessions were used in this study to reduce the threats to internal validity which can occur with this type of design.
Reliability observers were a special education teacher and one special education instructional assistant. Previously, the school psychologist trained both in making behavioral and educational observations. In addition, the special education teacher had received training in collecting reliability data from her university studies. The observers were instructed how to collect reliability data specific to this study.

The point-by-point method of reliability (number of agreements divided by the number of agreements plus disagreements multiplied by 100) was used to assess the student responses on worksheets during probe and baseline sessions (see Appendix G) (Tawney & Gast, 1984).

In order to compare the efficiency of two methods of addition, the researcher needed to follow the previously described plan with a high degree of accuracy. This plan was determined by conducting a task analysis of teaching the skill of addition for each method. This study checked for instrumentation effects by completing dependent and independent reliability 20% of the time and at least once per condition. Procedural reliability, which assessed the accuracy with which procedures during an intervention strategy were followed, was determined by the number of teacher behaviors observed for each instructional method (see Appendix K). The number of teacher behaviors observed was divided by the number of planned teacher behaviors multiplied by 100 (Billingsly, White, & Munson, 1980). One procedural reliability observation occurred during touchpoint acquisition instruction, with a 100% agreement. Procedural reliability data were collected on three occasions while teaching addition using touchpoints. The observations occurred once during Strategy 1, once during Strategy 2, and once during a
probe session using the control set. On each occasion, reliability was 100%. Procedural reliability was assessed twice for teaching addition with manipulatives—once each during Strategies 1 and 2. Procedural reliability for teaching addition with manipulatives was 100% accuracy. Seven observations occurred during probe sessions for an average accuracy of 97%.

**Social Validity**

Wolf (1978) suggested social validity be determined on three levels. The first is determining whether intervention goals are socially important. Students must master basic addition in order to be successful in higher-level math computation. Thus, all kindergarten, first and second grade students must learn addition as outlined in the curriculum document as well as Kentucky’s Learning Goals and Academic Expectations 1.5-1.9 (http://www.kde.state.ky.us/oapd/curric/Publications/Transformations/acadexp.html).

Wolf’s (1978) second level of social validity involves determining the social appropriateness of the procedures. Students use simple addition daily as a functional life skill. Also, Kentucky’s Core Content for Mathematics Assessment (MA-E-1.2.2) stated students must “add . . . whole numbers using a variety of methods” (http://www.kde.state.ky.us/oapd/curric/corecontent/mathematics_cc_30.asp).

The third level of social validity asked if the participants were satisfied with the results (Wolf, 1978). At the end of the study, the students were given a survey that asked which method, if any, they preferred to use while adding numbers.
Chapter Four: Data Analysis

Effectiveness of Touchpoints vs. Manipulatives

Doug. When Doug counted touchpoints on both numbers to add (Strategy 1; see Figure 1), his rate correct per minute showed a decreasing trend. In 5 probes, his correct rate per minute ranged from a high of 17 to a low of 10. As the increasing trend in Strategy 2 demonstrates, when Doug said the largest number and touched the touchpoints on the smaller number as he counted forward, there was a dramatic improvement. His correct rate per minute increased from 10 in the last probe using Strategy 1 to 19 digits correct when Doug used Strategy 2. Using Strategy 2, his digits correct per minute increased to a high of 33 on the 25th probe. As illustrated in Figure 1, the data paths for touchpoints, manipulatives, and the control set separated when Strategy 2 was implemented. Although the number of digits correct per minute was lower on probe 35 than on probe 32, the trend line was ascending. Doug’s average number of digits correct increased in each strategy from 14.5 in the first strategy to 28 in the second strategy and to 33.3 when touchpoints were added to the control set.

When Doug used manipulatives, his rate correct showed a slight ascending trend for the first strategy (using manipulatives for both numerals). His rate of digits correct per minute ranged from 9 to 20. During Strategy 2, the trend line of his performance was slightly ascending but his rate was lower than with touchpoints. Doug’s average during the second strategy was 15 digits correct in one minute.

Even though no instruction occurred, Doug’s rate correct on the control set significantly improved. The significant increase in correct digits per minute for the control set may have been influenced by his self-taught touchpoint strategy, or by his
increased speed in completing the worksheet. The increase also may have been due to the fact that numeral 1 is in that set. Analyses of Doug’s probe worksheets showed he completed more problems with an addend of one. During the second condition (Condition B), Doug was able to complete all probe worksheets with numeral one as an addend. On worksheets prior to that, Doug was unable to solve all the addition problems with an addend of one. Doug’s rate correct remained stable during Strategy 1 at 14 digits per minute. During Strategy 2, he steadily increased from a low of 11 to a high of 26. During probe 31 and 33, Doug was observed attempting to use touchpoints. Doug commented that he knew where the touchpoints were for numerals one, three, and four without the teacher showing him. Later in the study, when Doug was taught the touchpoints for numerals one and four for Condition C, he commented that he already knew them.

As Figure 1 shows, when using Strategy 1, there were no differences in Doug’s rate correct for touchpoints, manipulatives, or the control set. However, when Strategy 2 was introduced, Doug’s level of performance was substantially better using touchpoints. A significant separation of correct digits per minute occurred with Strategy 2, favoring touchpoints. In Condition C, touchpoints were taught for the numerals 1, 4, 5, and 9 (Set C numerals). A significant increase of the average number of correct digits increased from 21 to 33. The average of correct digits per minute was higher for any addition problem with which Doug used touchpoints.
Figure 1. Doug’s Probe Data
Keith. Similar to the trend in Doug’s data, the data representing Keith’s performance when adding with touchpoints showed a descending trend (see Figure 2). This trend reversed direction when the second strategy of adding more efficiently was implemented. The data for adding with touchpoints separated on probe 25 when Keith’s number of digits correct increased from 17 to 26. Moreover, when using this strategy, Keith’s lowest number of correct digits per minute was 13 on probe 20 and his highest was 43 on probe 35. Keith had the greatest success using the touchpoints the fast way (Strategy 2) than with any other method. In probes for Set A (touchpoint strategy), he occasionally skipped the fact 8+5 and 5+8. His average number of correct digits increased in each condition: baseline was 4; Strategy 1 was 9.67; the second strategy was 29.8; and when using touchpoints on the control set, it was 32.67.

This graph also shows an ascending trend during the second condition when adding with manipulatives. However, Keith’s rate correct was greater when adding with touchpoints the fast way (Strategy 2) than adding with manipulatives. The data for adding with touchpoints and adding with manipulatives did not overlap. Keith’s average digits correct in the second strategy using touchpoints was 29.8 compared to 24.4 for manipulatives. During probes, Keith skipped addition facts when he did not immediately know the answer.

In the second condition, Keith’s rate correct on the control set increased, even though no instruction occurred. He did not skip any facts. During Condition C when Keith used touchpoints with the control set, his rate correct increased from 24 digits correct per minute to 33 digits correct.

Anecdotal notes taken during probe sessions revealed that Keith memorized
several of the math facts in all sets. He was the most difficult student to monitor, as he did not touch the numerals when counting touchpoints. Instead, he looked at each touchpoint. The researcher was unable to detect whether Keith was using touchpoints or any other method during probes. Occasionally, Keith’s written answers were illegible. The researcher asked him what the numeral was and noted his response. These verbal responses were accepted as his answer.

When Keith used the touchpoint strategy on the control set, his correct responses increased at a greater rate (Condition C). The data show that Keith’s performance improved across all conditions. However, his rate correct was higher using touchpoints after Strategy 2 was introduced.
Figure 2. Keith’s Probe Data
Richard. The probe data in Figure 3 demonstrates the difficulty of determining which method of teaching simple addition worked best for Richard. During the first intervention strategy, his rate of correct responses using touchpoints and manipulatives decreased slightly, while his rate increased on the control set (Set C). His data for the control set did not overlap the other data during Strategy 1; it was consistently higher. Richard’s rate of correct digits per minute improved during the second strategy for both methods of instruction and the control set. His rate correct for touchpoints and manipulatives ran parallel; however, when using Strategy 2 with touchpoints, Richard’s rate of correct digits per minute was slightly higher than with manipulatives. This data for touchpoints separated and remained higher than any other method. During Strategy 2, Richard’s lowest number of correct digits per minute was 16 on probe 20 while the highest was 28.

The only notable increase occurred when Richard used touchpoints on the control set during Condition C. His number of digits correct increased from 24 to 31 when he added with touchpoints. When Richard used touchpoints for the numerals in the control set, his rate of correct digits per minute increased from an average of 23 per minute to 32. After learning to add the fast way (Strategy 2) with both strategies, Richard’s average of correct digits per minute was higher for any addition problem when he used touchpoints. Richard’s progress may have been affected by a one-week absence due to illness.
Figure 3. Richard’s Probe Data
Michael. During the first intervention strategy, Michael’s rate of correct digits per minute showed a descending trend when he added numbers with touchpoints. This reversed dramatically during the second strategy when he added touchpoints the fast way. His rate increased from a low of 10 digits correct per minute to a high of 41 digits correct per minute within four trials. Michael’s range of correct digits per minute went from a low of 4 on probe 12 (Strategy 1) to a high of 47 on probe 41 (control set).

With the control set, Michael’s rate of correct digits was greater than with either touchpoints or manipulatives until he learned to add with touchpoints the fast way (Strategy 2). His rate of correct numerals per minute increased when adding touchpoints the fast way and the data separated on probe 28. His average number of correct digits increased from 10.6 during Strategy 1 to 30 with Strategy 2. Similarly, Michael’s rate correct significantly increased with the control set after touchpoints were implemented, from 29.8 to 42.3 correct digits per minute.

When Michael added using manipulatives, his average correct digits decreased from Baseline (13 correct digits) to Strategy 1 (10 correct digits). He returned to the baseline average of 13 correct digits per minute when adding the fast way (Strategy 2).

When he used touchpoints with problems in the control set during Condition C, his average increased significantly from 30 correct digits per minute to 43 correct digits per minute. Michael’s average of correct digits increased when he used touchpoints the fast way with any set of addition problems.
Figure 4. Michael’s Probe Data
Rye. As shown in Figure 5, during the first strategy, Rye’s data for all methods of instruction overlapped. When Rye added with touchpoints, his data showed an increasing trend during Strategy 1. His lowest rate of digits correct per minute was 6 and his highest was 15. This trend continued at a greater rate when he added the fast way during Strategy 2. His performance ranged from 8 digits correct on probe 23 to 31 digits correct on probe 35. Rye’s data for adding with touchpoints separated from the data on other probe sets on probe 25. His average number of correct digits increased from a baseline of 7 to 11.5 during Strategy 1 and 20.6 while adding the fast way in Strategy 2.

When using manipulatives, Rye’s average correct rate increased from baseline to Strategy 1 but the trend line was descending. The trend line continued to decrease during Strategy 2 but at a slower rate than in the first strategy. His data range from a low of 3 to a high of 18. This data was not stable as it increased 10 digits between probes 21 and 24 then decreased 12 digits between probes 29 and 34.

Rye’s rate of digits correct per minute for the control set remained stable throughout Strategy 1 and Strategy 2. The lowest rate was 4 digits correct to a high of 8 digits correct. His rate correct for addition problems increased when the touchpoint method was introduced during Condition C, from 15 digits from 8 on probe 36 to 23 correct on probe 38. His rate of digits correct continued to increase with 29 digits and 33 digits on the last two probes.
Figure 5. Rye’s Probe Data
Tim. During Strategy 1, Tim’s data for both methods of instruction and the control set overlapped during between probes 4 and 14. The data for adding with touchpoints increased and separated on probe 15 with an increase of 13 digits, from 2 to 15 digits correct per minute.

Tim’s correct rate of digits per minute clearly increased when he added using touchpoints. The researcher once had to remind Tim to use touchpoints during the probes. As shown in Figure 6, his average number of correct digits increased steadily from 2 to 9.5 to 16 when adding with touchpoints during Strategy 1. Although his rate was lower during two probe sessions, he continued to improve with the second strategy. Tim’s range of correct digits per minute ranged from a low of 10 to a high of 20 during Strategy 2. Meanwhile, Tim’s average rate correct for adding with manipulatives remained stable and low (1.6, 3 respectively) throughout Strategy 1 and 2.

On the problems in the control set, Tim’s average number of correct digits was consistently low during baseline and intervention until touchpoints were used in Condition C. Tim’s range was a low of 1 to a high of 5 during both strategies. When touchpoints were used with the addition problems in the control set, his rate correct increased from 4 to 20 digits. Tim was absent two days and missed instruction and probe sessions 18 and 22. No remediation occurred and no probes were administered for these days.
Figure 6. Tim’s Probe Data
Efficiency of Touchpoints vs. Manipulatives

Table 2 shows the number of minutes each student needed to learn touchpoints placement to criterion. Keith required 2 minutes more than his peers to memorize touchpoint placement. He needed 1 additional minute each to master touchpoints on numeral 5 and 9. Instructional minutes required for the students to learn how to use manipulatives were minimal, as only one demonstration was needed.

Table 3 and Table 4 display individual times each student needed to meet criterion for each addition problem for touchpoints and manipulatives, respectively. Keith required more training time to reach mastery using both methods. He required 10 minutes more to master touchpoints and 7 minutes more for manipulatives. During the touchpoint method, he required 4 additional minutes to master 2+5, an additional 3 minutes to master 5+2, and 2 additional minutes for 2+8. When mastering manipulatives, Keith needed 4 additional minutes to learn 3+6, and 3 minutes for 6+3. Keith required additional minutes for the first 3 problems using touchpoints and the first 2 problems using manipulatives. The other students required the same amount of time to master adding with touchpoints (52 minutes) and for adding with manipulatives (58 minutes). On average, 53.7 minutes was needed to reach mastery for adding all problems using touchpoints while 59.2 minutes was required for adding using manipulatives. At first glance, it seems learning to add using touchpoints is more efficient. However, the time required to teach touchpoint placement must be added. When these minutes (average 19.4) are added, the total time for teaching touchpoints is 73.1 minutes compared to total time of 59.2 minutes for reaching mastery with manipulatives.
Table 2. Instructional minutes to criterion learning touchpoints

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Table 3. Instructional minutes to criterion using TouchMath

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<td>4</td>
<td>4</td>
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<tr>
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<td>7</td>
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<tr>
<td>Average time: 8.7 7.7 7.3 6 5 5 4 4 6</td>
<td>53.7</td>
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</table>
Table 4. Instructional minutes to criterion using manipulatives

<table>
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<tr>
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<th>3+6</th>
<th>6+3</th>
<th>3+7</th>
<th>7+3</th>
<th>6+7</th>
<th>7+6</th>
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<td>7</td>
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<td>6</td>
<td>5</td>
<td>6</td>
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<tr>
<td>Doug</td>
<td>8</td>
<td>7</td>
<td>7</td>
<td>7</td>
<td>6</td>
<td>6</td>
<td>5</td>
<td>6</td>
<td>6</td>
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<tr>
<td>Rye</td>
<td>8</td>
<td>7</td>
<td>7</td>
<td>7</td>
<td>6</td>
<td>6</td>
<td>5</td>
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<td>5</td>
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<td>Michael</td>
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<td>7</td>
<td>7</td>
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<tr>
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<td>8.7</td>
<td>7.5</td>
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<td>7</td>
<td>6</td>
<td>6</td>
<td>5</td>
<td>6</td>
<td>6</td>
<td>59.2</td>
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</table>

Student Preference for Touchpoints vs. Manipulatives

Table 5 displays the results of the student survey regarding which method, if any, they preferred. A student survey worksheet (see Appendix L) was completed. Each student circled the method, touchpoints or manipulatives, he preferred.

As they handed in the worksheet, each student was asked to explain his decision. Keith chose touchpoints and commented, “It does it faster.” Rye made the same comment about touchpoints while Doug stated, “It makes me go faster.” Richard explained that touchpoints “are easier.” Michael did not have a comment about why he picked touchpoints.

Tim was the only student who chose manipulatives, although his data showed that he performed better using touchpoints. When he was asked to explain his choice, Tim said he liked touchpoints. While trying to clarify Tim’s choice, the researcher demonstrated each method and asked if Tim liked adding with manipulatives or
touchpoints. Tim answered touchpoints. Later, the researcher again asked touchpoints or manipulatives. Tim replied manipulatives. It seemed Tim answered by repeating the last choice the researcher gave. This data on Table 5 reflects Tim’s original answer on the survey although his actions show he continued to use touchpoints

<table>
<thead>
<tr>
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<th>Touchpoints</th>
<th>Manipulatives</th>
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<tbody>
<tr>
<td>Keith</td>
<td>yes</td>
<td></td>
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<tr>
<td>Doug</td>
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<tr>
<td>Rye</td>
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<td>Richard</td>
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<td></td>
</tr>
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<td>Michael</td>
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<td></td>
</tr>
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<td>Tim</td>
<td></td>
<td>yes</td>
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<tr>
<td>Total</td>
<td>5</td>
<td>1</td>
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</tbody>
</table>
Chapter Five: Discussion

The first question addressed by this research was which is more effective, TouchMath or manipulatives in teaching basic addition facts to students with learning disabilities. Each student’s average number of digits correct per minute was greater when using touchpoints than when using manipulatives. Comparing the rate of correct digits between manipulatives and touchpoints, the difference ranged from a minimum of five (Richard: 24 digits with touchpoints; 19 digits with manipulatives) to a maximum of seventeen (Michael: 30 digits with touchpoints; 13 digits with manipulatives). When comparing trends of the individual student data, there were greater increasing trends with addition using touchpoints than addition with manipulatives. This improvement using touchpoints was evident during the second intervention strategy--adding the fast way, as well as during Condition C--teaching touchpoints for numerals in the control set. There was one exception. Comparison of Richard’s data between addition with touchpoints and manipulatives showed similar trend lines during the second intervention strategy. However, Richard’s average correct digits per minute showed he performed at a higher rate using touchpoints.

Five of the six students had behavior goals on their Individual Education Programs. The only difference noted in the data between Keith, who did not have behavior goals, and the other students, is that Keith required more instructional time to master touchpoints, adding with touchpoints, and adding with manipulatives. Anecdotal notes show all students were on task and required no behavioral intervention. All students increased their fluency rate in simple addition.

The second question asked was which method was more time efficient in teaching
basic addition facts to students with learning disabilities. The average time for a student to acquire touchpoint placement and adding each math fact in Set A with touchpoints was 73.1 minutes. The average time for a student to add each math fact in Set B using manipulatives was 59.2 minutes. Learning to add using manipulatives was 13.9 minutes faster on average than learning touchpoints for three numerals and adding using touchpoints. However, when comparing just adding and eliminating the time to master touchpoint placement, it was quicker to add with touchpoints (53.7 minutes) than with manipulatives (59.2). This difference may be due to the time required to move three-dimensional manipulatives into place. For a total comparison, adding with manipulatives had an initial advantage over adding with touchpoints. However, this advantage may be lost over time.

The third research question addressed student’s opinions regarding both instructional procedures. When the students were asked which method, if any, they preferred, 5 of 6 chose adding with touchpoints. Tim was the only student who said he preferred using manipulatives when he added. Although Tim’s performance demonstrates he has a much higher rate of accuracy using touchpoints and he verbally changed his preference of method, Tim’s original answer is indicated on Table 5. After the students learned the touchpoints for Set A, a few continued to ask for the touchpoints for numerals in the other sets. When they were not provided, one student created his own touchpoints for the numerals. After completing the survey, each student was asked why he preferred a particular method. All students selecting touchpoints said in some manner that is was faster and easier.

Of the three research questions, the results favored adding simple equations using
the TouchMath method was preferred on two. Using the TouchMath method resulted in a higher rate of correct digits per minute and was more preferred than adding with manipulatives. Adding with manipulatives was a few minutes faster than learning to add with touchpoints. This advantage may be lost as students gain fluency, because time is no longer required to teach the placement of touchpoints on numerals.

Limitations

Several limitations of this study may have affected the results. First, the control set was not equivalent to the other two sets due to numerals one and nine being in that set. These were the easiest and hardest numbers to add; therefore, they should not have been in the same set. Another limitation was the unequal number of unique facts in each probe worksheet. In probe worksheet A, 2+5 was presented two times. The following problems were listed six times: 5+2, 2+8, and 5+8. These problems were listed four times: 8+2, 8+5, 2+2, 5+5, and 8+8. Other probes for the different sets had a similar pattern. The back of the probe worksheets was a duplicate of the front. This compounded the problem of unequal representation of each fact. Although students did not indicate that they were aware of the duplication, it was possible that they memorized the order of some answers.

Another problem created by using only three numerals in each set was the limited variety of answers. For example, the only answers for set A were 7, 10, 13, 4, and 16. Again, the students did not seem to be aware of this pattern, as they used other answers to solve the math problems, but it could have contributed to memorizing the sums. Another limitation of the study was implementing Strategy 2 following the exact directions in the teacher’s manual. The method the manual recommends to increase fluency is to place manipulatives or draw circles beside the smaller number. In order to be more consistent
with Strategy 2 touchpoint method, drawing only circles should have been used. Drawing circles and using touchpoints would be consistent semi-concrete level as described by Mercer (1997) while using three-dimensional counters is a concrete level.

Another limitation of this study was the failure to document the time students spent learning to add with manipulatives. While time required to master touchpoint acquisition was documented, the time required to master how manipulatives were used to add was not. The time was minimal but documentation was needed for comparison.

Finally, although the results of this study support TouchMath as an effective and student preferred method of adding. However because the school year ended, this study does not provide generalization and maintenance data to support its use over time and across settings.

**Implications for Future Research**

This study is one small step toward building the external validity (Birnbrauer, 1981) of the TouchMath method of teaching addition. While touchpoints were better than manipulatives for developing single digit math fluency, it may not generalize to other operations or to higher-level addition skills. This study does not support using only touchpoints for understanding the function of addition. Previous instruction for these students included simple addition story problems, which used three-dimensional figures (sheep, cows, ducks, etc.) to act out the story. In this study, TouchMath was used for fluency and accuracy, not for number sense in addition. Similar studies should continue this research to establish data on generalization and maintenance to support the use of TouchMath across settings and over time. Although this study showed touchpoints were effective with this group of students with learning and behavior problems, a more
thorough investigation is needed to document its effectiveness on students with a variety of behavioral difficulties. Further research also is needed to establish effectiveness across students of all ages as well as with various disabilities.

Other products from Innovative Learning Concepts, Inc. use touchpoints for subtraction, multiplication, and division. Results from this study on addition cannot be generalized to other operations using touchpoints. I prefer using touchpoints for students who understand the concept of addition and subtraction but have difficulty memorizing addition and subtraction facts. I do not use touchpoints with students needing to memorize multiplication facts. If students are required to memorize, I prefer they memorize the actual multiplication facts instead of memorizing skip counting in order to use touchpoints. External validity is needed for the various operations. After external validity is established for effectiveness with these operations, further research is needed comparing efficiency between instructional methods (i.e., manipulatives) across students, skills, and settings.

Following Miller and Mercer’s (1997a) call for professional educators to seek practices that provide “the best results in the shortest amount of time” (p. 54.), a more thorough investigation is needed to compare the efficiency of different strategies. TouchMath should also be compared to other effective strategies to determine which is more efficient. No study of relative efficiencies would be complete if it only considered two options, all effective strategies should be compared.
Appendix A

Touchpoint Counting Patterns
Appendix A

Touchpoint Counting Patterns
Touchpoints

The one is touched at the top while counting: “One.”

The two is touched at the beginning and the end of the numeral while counting: “One, two.”

The three is touched at the beginning, middle and end of the numeral while counting, “One, two, three.”

The four is touched and counted from top to bottom on the down strokes while counting: “One, two, three, four.”

The five is touched and counted in the sequential order pictured: “One, two, three, four, five.” To help in remembering the fourth Touchpoint, it may be referred to as the “belly button”.
The six begins the use of dots with circles. The encircled dots should be touched and counted twice, whenever they appear. Six is touched and counted from top to bottom: “One-two, three-four, five-six.”

The seven is touched and counted from top to bottom: “One-two, three-four, five-six,” followed by the single dot “seven.” The single Touchpoint can be thought of as the nose. Teachers sometimes tell young or remedial students to, “touch him on the nose” to help them remember the final touchpoint.

The eight is touched and counted from left to right: “One-two, three-four, five-six, seven-eight.” Tell the young or remedial students that the eight looks like a robot. Count his head first, and then his body.

The nine is touched and counted from top to bottom: “One-two, three-four, five-six, seven-eight,” followed by the single dot: “nine.” Tell the young or remedial student that the nine is the only number with a “hat”. They should begin counting at the hat and continue straight down the body. Again, the single Touchpoint can be thought of as the nose.
APPENDIX B

Addition Sets
Using TOUCH MATH techniques
Numerals 2, 5, 7, 8, 10, 2, 24, 12

Addition Sets

SET A

The computer

Control Set

Numerals 1, 4, 9

Addition Sets
APPENDIX C

Set A Probe Worksheet Sample

(Student worksheets were printed on the front and back of one paper.)
5 + 2

2 + 8

8 + 2

5 + 8

8 + 5

2 + 5

8 + 2

5 + 8

2 + 8

8 + 8

5 + 5

2 + 2

2 + 2

5 + 5

2 + 2

APPENDIX D

Set B Probe Worksheet Sample

(Student worksheets were printed on the front and back of one paper.)
Set B Probe Worksheet
Name: _______________
Total time: ____________

6 + 6
6 + 6
3 + 3
3 + 6
7 + 3
7 + 6
7 + 7
6 + 3
6 + 7
3 + 7
3 + 3
APPENDIX E

Set C Probe Worksheet Sample

(Student worksheets were printed on the front and back of one paper.)
Set C Probe Worksheet
Name:_______________

# digits correct
in one minute:_________

1 + 4 = 4 + 4 = 9 + 4 = 1 + 9 = 4 + 9 = 9 + 4 =
APPENDIX F

Classroom Discipline Procedure
CONSEQUENCES

Listed below are the consequences for inappropriate behavior. It is the middle component of the classroom discipline plan (Wong, 1998). Also posted are the rules and rewards. The consequences component is adapted from 1, 2, 3 Magic: Effective Discipline for Children 2-12 (1995).

Step 1: “That’s 1”
Step 2: “That’s 2”
Step 3: “That’s 3...time out” Time out is 2 minutes. The timer starts when the time out rules are followed.
Step 4: When the timer dings, the student is allowed to resume normal class duties. If the student continues inappropriate behavior, time out begins again for 2 minutes.

TIME OUT RULES
Teacher doesn’t hear you.
Teacher doesn’t see you.
APPENDIX G

Reliability of Student Response for Baseline and Probe Sessions

Sample for Set A Worksheet # 1

Sample for Set B Worksheet # 1
Summary of Student Response for Probe Sessions  
Set A Worksheet # 1

Instructor:  **LuAnne Littlefield**  
Student: ___________________  
Reliability observer: ________________

Mark  + correct answer  
- incorrect answer

The printer numerals are the correct answers to Probe A worksheet # 1. 
The second row indicates the researcher’s data collection. 
The last row indicates reliability observer’s data for student responses.

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<td>1 3 1 6 1 0 1 0</td>
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**TOTAL INCORRECT:** ______
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Number of agreements:__________

Divided by Number of agreements + disagreements:__________

\[ \times 100 \]

Reliability percentage:__________
Summary of Student Response for Probe Sessions  
Set B Worksheet #1

Instructor: LuAnne Littlefield

Student:_________________

Reliability observer:______________

Mark + correct answer
- incorrect answer

The printer numerals are the correct answers to Probe B worksheet #1.
The second row indicates the researcher’s data collection.
The last row indicates reliability observer’s data for student responses.

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<td>Row 3</td>
<td>1 0 1 2 6 9</td>
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<td>Row 5</td>
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TOTAL INCORRECT:_____
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Number of agreements: 
Divided by Number of agreements + disagreements:

\[ \times 100 \]

Reliability percentage:
APPENDIX H

Student Response for Touchpoint Acquisition
Student Response for Touchpoint Acquisition

Instructor: **LuAnne Littlefield**  
Date: _______

**NOTES:**  
Criterion = 100% accuracy on 5 consecutive trials.  
Maximum of 2 numbers/session  
All students must reach mastery to add new number.  
All students must master all numbers before teaching addition.

Mark  + for correct pattern performed independently  
- incorrect pattern or assistance needed

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</table>

Touchpoint numerals to be introduced tomorrow: ______________

Students who need tutoring: ______________
APPENDIX I

Sample lesson plan teaching with touchpoints
APPENDIX J

Sample lesson plan for teaching addition with manipulatives
APPENDIX K

Procedural Reliability Procedures

Sample one- Probe Sessions

Sample two- Touchpoint Acquisition

Sample three- Addition with Manipulatives

Sample four- Addition with Touchpoints
Procedural Reliability for Probes

Observer: __________________________

Date: __________

Pretest:

Mark when the planned procedure is observed.

☐ Introduce pretest

Student instructions:

☐ OK to not get answers correct
☐ Don’t count on fingers
☐ Don’t use tally marks for counting
☐ If don’t know answer, skip to the next problem and put a slash mark for the answer.
☐ Practice pencil up when timer dings.
☐ Position students—separate
☐ Pass out materials
☐ Give signal to begin.
☐ Monitor work, encourage.
☐ Praise pencils up when timer dings.
☐ Direct students to write name on paper.
☐ Collect papers.

Number of steps observed: _______

Divided by the number of planned steps: 13

X 100

Procedural reliability percentage for baseline: _______
Procedural Reliability for Touchpoint Acquisition

Observer: ____________________________

Date: __________

Touchpoint Acquisition

*Mark when the planned procedure is observed.*

☐ Attentional cue given.

☐ Teacher models touchpoint

☐ Students participate as teacher touches touchpoints.

☐ Teacher passes out materials.

☐ Teacher prompts practice trials.

☐ Students practice activity.

☐ Teacher praises or redirects.

☐ Students continue to practice until teacher gives other directions.

☐ Teacher collects data.

Number of steps observed: _______

Divided by the number of planned steps: 9

X 100

Procedural reliability percentage for baseline: _______
Procedural Reliability for Addition with Manipulatives

Observer: _______________________________

Date:___________

Addition with Manipulatives

Mark when the planned procedure is observed.

☐ Probe data collected.

☐ Attentional cue given.

☐ Teacher reviews addition with manipulatives.

☐ Teacher models addition using manipulatives.

☐ Students participate as teacher adds using manipulatives.

☐ Teacher passes out materials.

☐ Teacher prompts practice trials.

☐ Students practice activity.

☐ Teacher praises or redirects.

☐ Students continue to practice until teacher gives other direction.

☐ Teacher collects data.

☐ Teacher passes out materials.

☐ Teacher prompts practice trials.

☐ Students practice activity.

☐ Teacher praises or redirects.

☐ Students continue to practice until teacher gives other direction.

☐ Teacher collects data.

Number of steps observed: _______

Divided by the number of planned steps: 17

X 100

Procedural reliability percentage for baseline: _______
Procedural Reliability for Addition with Touchpoints

Observer: _______________________________

Date: __________

Touchpoint Addition

Mark when the planned procedure is observed.

☐ Attentional cue given.

☐ Teacher reviews touchpoints on numerals.

☐ Teacher models addition using touchpoints on numerals.

☐ Students participate as teacher touches touchpoints to add.

☐ Teacher passes out materials.

☐ Teacher prompts practice trials.

☐ Students practice activity.

☐ Teacher praises or redirects.

☐ Students continue to practice until teacher gives other direction.

☐ Teacher collects data.

☐ Teacher models addition using touchpoints but no touchpoints are on the numerals.

☐ Students participate as teacher touches touchpoints to add.

☐ Teacher passes out materials.

☐ Teacher prompts practice trials.

☐ Students practice activity.

☐ Teacher praises or redirects.

☐ Students continue to practice until teacher gives other direction.

☐ Teacher collects data.

Number of steps observed: ______

Divided by the number of planned steps: 18

\[ \times 100 \]

Procedural reliability percentage for baseline: ______
APPENDIX L

Student Survey
Circle the one you like to use the best.

I like to add using touchpoints.

\[ \begin{array}{c}
5 \\
+ 3 \\
\hline
\end{array} \]

I like to add using counters.

\[ \begin{array}{c}
5 \cdot \cdot \cdot \cdot \cdot \\
+ 3 \cdot \cdot \cdot \\
\hline
\end{array} \]
References


Education and Training of the Mentally Retarded, 8, 140-144.


Learning Disability Quarterly, 5, 305-311.


References


